

**1-1.**

Round off the following numbers to three significant figures: (a) 3.45555 m, (b) 45.556 s, (c) 5555 N, (d) 4525 kg.

**SOLUTION**

(a) 3.46 m    (b) 45.6 s    (c) 5.56 kN    (d) 4.52 Mg

**Ans.**

**Ans:**  
a) 3.46 m  
b) 45.6 s  
c) 5.56 kN  
d) 4.52 Mg

1-2.

Represent each of the following combinations of units in the correct SI form using an appropriate prefix:

(a) Mg/mm, (b) mN / $\mu$ s, (c)  $\mu$ m  $\cdot$  Mg.

### SOLUTION

a)  $\text{kN}/\mu\text{s} = 10^3\text{N}/(10^{-6})\text{s} = \text{GN}/\text{s}$

**Ans.**

b)  $\text{Mg}/\text{mN} = 10^6\text{g}/10^{-3}\text{N} = \text{Gg}/\text{N}$

**Ans.**

c)  $\text{MN}/(\text{kg} \cdot \text{ms}) = 10^6\text{N}/\text{kg}(10^{-3}\text{s}) = \text{GN}/(\text{kg} \cdot \text{s})$

**Ans.**

**Ans:**

a) GN/s

b) Gg/N

c) GN/(kg  $\cdot$  s)

1-3.

Represent each of the following combinations of units in the correct SI form using an appropriate prefix: (a) Mg/mm, (b) mN/ $\mu$ s, (c)  $\mu$ m  $\cdot$  Mg.

### SOLUTION

$$a) \text{ Mg/mm} = \frac{10^3 \text{ kg}}{10^{-3} \text{ m}} = \frac{10^6 \text{ kg}}{\text{m}} = \text{Gg/m}$$

**Ans.**

$$b) \text{ mN}/\mu\text{s} = \frac{10^{-3} \text{ N}}{10^{-6} \text{ s}} = \frac{10^3 \text{ N}}{\text{s}} = \text{kN/s}$$

**Ans.**

$$c) \mu\text{m} \cdot \text{Mg} = [10^{-6} \text{ m}] \cdot [10^3 \text{ kg}] = (10)^{-3} \text{ m} \cdot \text{kg} \\ = \text{mm} \cdot \text{kg}$$

**Ans.**

**Ans:**  
a) Gg/m  
b) kN/s  
c) mm  $\cdot$  kg

\*1-4.

What is the weight in newtons of an object that has a mass of (a) 8 kg, (b) 0.04 kg, and (c) 760 Mg?

### SOLUTION

a)  $W = 9.81(8) = 78.5 \text{ N}$

**Ans.**

b)  $W = 9.81(0.04)(10^{-3}) = 3.92(10^{-4}) \text{ N} = 0.392 \text{ mN}$

**Ans.**

c)  $W = 9.81(760)(10^3) = 7.46(10^6) \text{ N} = 7.46 \text{ MN}$

**Ans.**

**Ans:**

a)  $W = 78.5 \text{ N}$

b)  $W = 0.392 \text{ mN}$

c)  $W = 7.46 \text{ MN}$

**1-5.**

Represent each of the following as a number between 0.1 and 1000 using an appropriate prefix: (a) 45320 kN, (b)  $568(10^5)$  mm, and (c) 0.00563 mg.

**SOLUTION**

a)  $45\,320\text{ kN} = 45.3\text{ MN}$

**Ans.**

b)  $568(10^5)\text{ mm} = 56.8\text{ km}$

**Ans.**

c)  $0.00563\text{ mg} = 5.63\ \mu\text{g}$

**Ans.**

**Ans:**

a) 45.3 MN

b) 56.8 km

c) 5.63  $\mu\text{g}$

1-6.

Round off the following numbers to three significant figures: (a) 58 342 m, (b) 68.534 s, (c) 2553 N, and (d) 7555 kg.

### SOLUTION

a) 58.3 km    b) 68.5 s    c) 2.55 kN    d) 7.56 Mg

**Ans.**

**Ans:**  
a) 58.3 km  
b) 68.5 s  
c) 2.55 kN  
d) 7.56 Mg

1-7.

Represent each of the following quantities in the correct SI form using an appropriate prefix: (a) 0.000 431 kg, (b)  $35.3(10^3)$  N, and (c) 0.005 32 km.

### SOLUTION

a)  $0.000\ 431\ \text{kg} = 0.000\ 431(10^3)\ \text{g} = 0.431\ \text{g}$

**Ans.**

b)  $35.3(10^3)\ \text{N} = 35.3\ \text{kN}$

**Ans.**

c)  $0.005\ 32\ \text{km} = 0.005\ 32(10^3)\ \text{m} = 5.32\ \text{m}$

**Ans.**

**Ans:**  
a) 0.431 g  
b) 35.3 kN  
c) 5.32 m

\*1-8.

Represent each of the following combinations of units in the correct SI form: (a) Mg/ms, (b) N/mm, and (c) mN/(kg·μs).

### SOLUTION

$$\text{a) } \frac{\text{Mg}}{\text{ms}} = \frac{10^3 \text{ kg}}{10^{-3} \text{ s}} = 10^6 \text{ kg/s} = \text{Gg/s}$$

**Ans.**

$$\text{b) } \frac{\text{N}}{\text{mm}} = \frac{1 \text{ N}}{10^{-3} \text{ m}} = 10^3 \text{ N/m} = \text{kN/m}$$

**Ans.**

$$\text{c) } \frac{\text{mN}}{(\text{kg} \cdot \mu\text{s})} = \frac{10^{-3} \text{ N}}{10^{-6} \text{ kg} \cdot \text{s}} = \text{kN}/(\text{kg} \cdot \text{s})$$

**Ans.**

**Ans:**

a) Gg/s

b) kN/m

c) kN/(kg·s)



**1-9.**

Represent each of the following combinations of units in the correct SI form using an appropriate prefix: (a) m/ms, (b)  $\mu\text{km}$ , (c) ks/mg, and (d)  $\text{km} \cdot \mu\text{N}$ .

**SOLUTION**

a)  $\text{m/ms} = \left( \frac{\text{m}}{(10)^{-3} \text{s}} \right) = \left( \frac{(10)^3 \text{m}}{\text{s}} \right) = \text{km/s}$  **Ans.**

b)  $\mu\text{km} = (10)^{-6}(10)^3 \text{m} = (10)^{-3} \text{m} = \text{mm}$  **Ans.**

c)  $\text{ks/mg} = \left( \frac{(10)^3 \text{s}}{(10)^{-6} \text{kg}} \right) = \left( \frac{(10)^9 \text{s}}{\text{kg}} \right) = \text{Gs/kg}$  **Ans.**

d)  $\text{km} \cdot \mu\text{N} = [(10)^3 \text{m}][(10)^{-6} \text{N}] = (10)^{-3} \text{m} \cdot \text{N} = \text{mm} \cdot \text{N}$  **Ans.**

**Ans:**  
a) km/s  
b) mm  
c) Gs/kg  
d) mm · N

**1-10.**

Represent each of the following combinations of units in the correct SI form using an appropriate prefix:

(a)  $\text{GN} \cdot \mu\text{m}$ , (b)  $\text{kg}/\mu\text{m}$ , (c)  $\text{N}/\text{ks}^2$ , (d)  $\text{kN}/\mu\text{s}$

**SOLUTION**

a)  $\text{GN} \cdot \mu\text{m} = 10^9(10^{-6}) \text{N} \cdot \text{m} = \text{kN} \cdot \text{m}$

**Ans.**

b)  $\text{kg}/\mu\text{m} = 10^3 \text{g}/10^{-6} \text{m} = \text{Gg}/\text{m}$

**Ans.**

c)  $\text{N}/\text{ks}^2 = \text{N}/10^6 \text{s}^2 = 10^{-6} \text{N}/\text{s}^2 = \mu\text{N}/\text{s}^2$

**Ans.**

d)  $\text{kN}/\mu\text{s} = 10^3 \text{N}/10^{-6} \text{s} = 10^9 \text{N}/\text{s} = \text{GN}/\text{s}$

**Ans.**

**Ans:**

- a)  $\text{kN} \cdot \text{m}$
- b)  $\text{Gg}/\text{m}$
- c)  $\mu\text{N}/\text{s}^2$
- d)  $\text{GN}/\text{s}$

**1-11.**

Represent each of the following combinations of units in the correct SI form using an appropriate prefix: (a)  $\mu\text{MN}$ , (b)  $\text{N}/\mu\text{m}$ , (c)  $\text{MN}/\text{ks}^2$ , and (d)  $\text{kN}/\text{ms}$ .

**SOLUTION**

a)  $\mu\text{MN} = 10^{-6}(10^6) \text{ N} = \text{N}$

**Ans.**

b)  $\frac{\text{N}}{\mu\text{m}} = \frac{\text{N}}{10^{-6} \text{ m}} = 10^6 \text{ N/m} = \text{MN/m}$

**Ans.**

c)  $\frac{\text{MN}}{\text{ks}^2} = \frac{10^6 \text{ N}}{(10^3)^2 \text{ s}^2} = \text{N/s}^2$

**Ans.**

d)  $\frac{\text{kN}}{\text{ms}} = \frac{10^3 \text{ N}}{10^{-3} \text{ s}} = 10^6 \frac{\text{N}}{\text{s}} = \text{MN/s}$

**Ans.**

**Ans:**  
a) N  
b) MN/m  
c) N/s<sup>2</sup>  
d) MN/s

\*1-12.

Water has a density of  $1.94 \text{ slug/ft}^3$ . What is the density expressed in SI units? Express the answer to three significant figures.

## SOLUTION

Using Table 1-2, we have

$$\begin{aligned}\rho_w &= \left(\frac{1.94 \text{ slug}}{\text{ft}^3}\right) \left(\frac{14.5938 \text{ kg}}{1 \text{ slug}}\right) \left(\frac{1 \text{ ft}^3}{0.3048^3 \text{ m}^3}\right) \\ &= 999.8 \text{ kg/m}^3 = 1.00 \text{ Mg/m}^3\end{aligned}$$

**Ans.**

**Ans:**  
 $\rho_w = 1.00 \text{ Mg/m}^3$

**1–13.**

The density (mass/volume) of aluminum is 5.26 slug/ft<sup>3</sup>. Determine its density in SI units. Use an appropriate prefix.

**SOLUTION**

$$\begin{aligned} 5.26 \text{ slug/ft}^3 &= \left( \frac{5.26 \text{ slug}}{\text{ft}^3} \right) \left( \frac{\text{ft}}{0.3048 \text{ m}} \right)^3 \left( \frac{14.59 \text{ kg}}{1 \text{ slug}} \right) \\ &= 2.71 \text{ Mg/m}^3 \end{aligned}$$

**Ans.**

**Ans:**  
2.71 Mg/m<sup>3</sup>

**1–14.**

Evaluate each of the following to three significant figures and express each answer in SI units using an appropriate prefix:

(a)  $(212 \text{ mN})^2$ , (b)  $(52800 \text{ ms})^2$ , and (c)  $[548(10^6)]^{1/2} \text{ ms}$ .

**SOLUTION**

a)  $(212 \text{ mN})^2 = [212(10)^{-3} \text{ N}]^2 = 0.0449 \text{ N}^2 = 44.9(10)^{-3} \text{ N}^2$  **Ans.**

b)  $(52\,800 \text{ ms})^2 = [52\,800(10)^{-3}]^2 \text{ s}^2 = 2788 \text{ s}^2 = 2.79(10^3) \text{ s}^2$  **Ans.**

c)  $[548(10^6)]^{1/2} \text{ ms} = (23\,409)(10)^{-3} \text{ s} = 23.4(10)^3(10)^{-3} \text{ s} = 23.4 \text{ s}$  **Ans.**

**Ans:**  
a)  $44.9(10)^{-3} \text{ N}^2$   
b)  $2.79(10^3) \text{ s}^2$   
c)  $23.4 \text{ s}$

**1–15.**

Using the SI system of units, show that Eq. 1–2 is a dimensionally homogeneous equation which gives  $F$  in newtons. Determine to three significant figures the gravitational force acting between two spheres that are touching each other. The mass of each sphere is 200 kg and the radius is 300 mm.

**SOLUTION**

Using Eq. 1–2,

$$F = G \frac{m_1 m_2}{r^2}$$

$$N = \left( \frac{\text{m}^3}{\text{kg} \cdot \text{s}^2} \right) \left( \frac{\text{kg} \cdot \text{kg}}{\text{m}^2} \right) = \frac{\text{kg} \cdot \text{m}}{\text{s}^2} \quad (\mathbf{Q.E.D.})$$

$$F = G \frac{m_1 m_2}{r^2}$$

$$= 66.73(10^{-12}) \left[ \frac{200(200)}{0.6^2} \right]$$

$$= 7.41(10^{-6}) \text{ N} = 7.41 \mu\text{N}$$

**Ans.**

**Ans:**  
7.41  $\mu\text{N}$

**\*1-16.**

Evaluate each of the following to three significant figures and express each answer in SI units using an appropriate prefix: (a)  $(200 \text{ kN})^2$ , (b)  $(0.005 \text{ mm})^2$ , and (c)  $(400 \text{ m})^3$ .

**SOLUTION**

a)  $(200 \text{ kN})^2 = 40\,000(10^6) \text{ N}^2 = 0.04(10^{12}) \text{ N}^2 = 0.04 \text{ MN}^2$

**Ans.**

b)  $(0.005 \text{ mm})^2 = 25(10^{-12}) \text{ m}^2 = 25\mu\text{m}^2$

**Ans.**

c)  $(400 \text{ m})^3 = 0.064(10^9) \text{ m}^3 = 0.064 \text{ km}^3$

**Ans.**

**Ans:**

a)  $0.04 \text{ MN}^2$

b)  $25\mu\text{m}^2$

c)  $0.064 \text{ km}^3$



1-17.

If a car is traveling at 55 mi/h, determine its speed in kilometers per hour and meters per second.

### SOLUTION

$$55 \text{ mi/h} = \left(\frac{55 \text{ mi}}{1 \text{ h}}\right)\left(\frac{5280 \text{ ft}}{1 \text{ mi}}\right)\left(\frac{0.3048 \text{ m}}{1 \text{ ft}}\right)\left(\frac{1 \text{ km}}{1000 \text{ m}}\right)$$
$$= 88.5 \text{ km/h} \quad \text{Ans.}$$

$$88.5 \text{ km/h} = \left(\frac{88.5 \text{ km}}{1 \text{ h}}\right)\left(\frac{1000 \text{ m}}{1 \text{ km}}\right)\left(\frac{1 \text{ h}}{3600 \text{ s}}\right) = 24.6 \text{ m/s} \quad \text{Ans.}$$

**Ans:**  
88.5 km/h  
24.6 m/s

**1–18.**

Evaluate  $(204 \text{ mm})(0.00457 \text{ kg})/(34.6 \text{ N})$  to three significant figures and express the answer in SI units using an appropriate prefix.

**SOLUTION**

$$\begin{aligned}(204 \text{ mm})(0.00457 \text{ kg})/(34.6 \text{ N}) &= \left( \frac{[204(10^{-3}) \text{ m}][4.57(10^{-3}) \text{ kg}]}{34.6 \text{ N}} \right) \\ &= \left( \frac{26.9(10^{-6}) \text{ m} \cdot \text{kg}}{1 \text{ N}} \right) \\ &= 26.9 \mu\text{m} \cdot \text{kg/N}\end{aligned}$$

**Ans.**

**Ans:**  
 $26.9 \mu\text{m} \cdot \text{kg/N}$

**1–19.**

The specific weight (wt./vol.) of brass is 520 lb/ft<sup>3</sup>. Determine its density (mass/vol.) in SI units. Use an appropriate prefix.

**SOLUTION**

$$\begin{aligned} 520 \text{ lb/ft}^3 &= \left( \frac{520 \text{ lb}}{\text{ft}^3} \right) \left( \frac{1 \text{ ft}}{0.3048 \text{ m}} \right)^3 \left( \frac{4.448 \text{ N}}{1 \text{ lb}} \right) \left( \frac{1 \text{ kg}}{9.81 \text{ N}} \right) \\ &= 8.33 \text{ Mg/m}^3 \end{aligned}$$

**Ans.**

**Ans:**  
8.33 Mg/m<sup>3</sup>

**\*1–20.**

If a man weighs 155 lb on earth, specify (a) his mass in slugs, (b) his mass in kilograms, and (c) his weight in newtons. If the man is on the moon, where the acceleration due to gravity is  $g_m = 5.30 \text{ ft/s}^2$ , determine (d) his weight in pounds, and (e) his mass in kilograms.

### SOLUTION

$$\text{a) } m = \frac{155}{32.2} = 4.81 \text{ slug}$$

**Ans.**

$$\text{b) } m = 155 \left[ \frac{14.59 \text{ kg}}{32.2} \right] = 70.2 \text{ kg}$$

**Ans.**

$$\text{c) } W = 155(4.4482) = 689 \text{ N}$$

**Ans.**

$$\text{d) } W = 155 \left[ \frac{5.30}{32.2} \right] = 25.5 \text{ lb}$$

**Ans.**

$$\text{e) } m = 155 \left[ \frac{14.59 \text{ kg}}{32.2} \right] = 70.2 \text{ kg}$$

**Ans.**

Also,

$$m = 25.5 \left[ \frac{14.59 \text{ kg}}{5.30} \right] = 70.2 \text{ kg}$$

**Ans.**

**Ans:**

- a) 4.81 slug
- b) 70.2 kg
- c) 689 N
- d) 25.5 lb
- e) 70.2 kg

**1-21.**

Two particles have a mass of 8 kg and 12 kg, respectively. If they are 800 mm apart, determine the force of gravity acting between them. Compare this result with the weight of each particle.

**SOLUTION**

$$F = G \frac{m_1 m_2}{r^2}$$

Where  $G = 66.73(10^{-12}) \text{ m}^3/(\text{kg} \cdot \text{s}^2)$

$$F = 66.73(10^{-12}) \left[ \frac{8(12)}{(0.8)^2} \right] = 10.0(10^{-9}) \text{ N} = 10.0 \text{ nN}$$

**Ans.**

$$W_1 = 8(9.81) = 78.5 \text{ N}$$

**Ans.**

$$W_2 = 12(9.81) = 118 \text{ N}$$

**Ans.**

**Ans:**

$$F = 10.0 \text{ nN}$$

$$W_1 = 78.5 \text{ N}$$

$$W_2 = 118 \text{ N}$$

**2-1.**

Determine the magnitude of the resultant force  $\mathbf{F}_R = \mathbf{F}_1 + \mathbf{F}_2$  and its orientation  $\theta$ , measured counterclockwise from the positive  $x$  axis.

**SOLUTION**

**Sine Law:**

$$\frac{\sin 67.62^\circ}{320} = \frac{\sin (45^\circ + \alpha)}{260} \quad \alpha = 3.728^\circ$$

$$\theta = 180^\circ - \alpha = 176^\circ$$

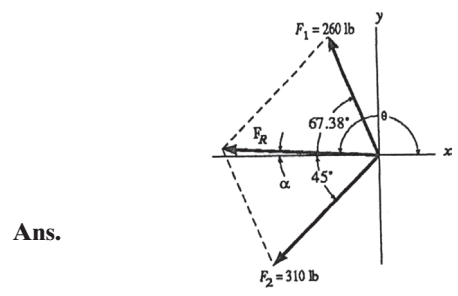
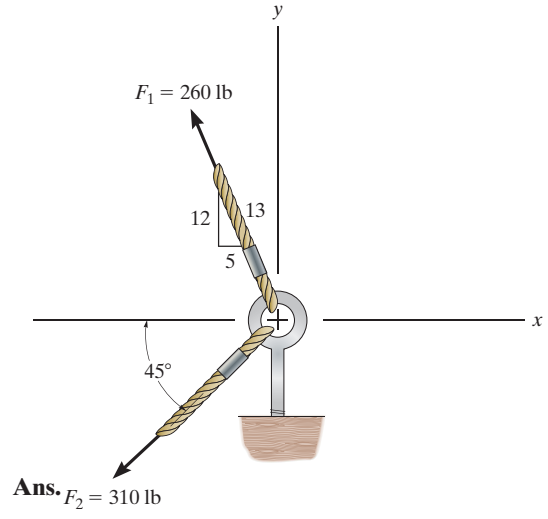
$$\tan^{-1} \frac{12}{5} = 67.38^\circ$$

$$67.38^\circ + 45^\circ = 112.38^\circ$$

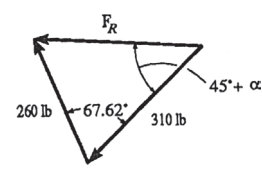
$$\frac{360^\circ - \alpha (112.38^\circ)}{\alpha} = 67.62^\circ$$

**Cosine Law:**

$$F_R = \sqrt{310^2 + 260^2 - 2(310)(260) \cos 67.62^\circ} = 320 \text{ lb}$$



**Ans.**



**Ans:**  
 $F_R = 320 \text{ lb}$   
 $\theta = 176^\circ$

2-2.

Determine the magnitude of the resultant force  $\mathbf{F}'_R = \mathbf{F}_1 - \mathbf{F}_2$  and its orientation  $\theta$ , measured counterclockwise from the positive  $x$  axis.

**SOLUTION**

$$\tan^{-1} \frac{12}{5} = 67.38^\circ$$

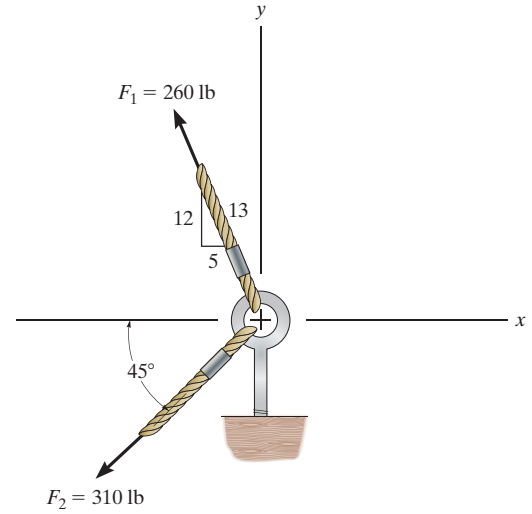
$$67.38^\circ + 45^\circ = 112.38^\circ$$

**Cosine Law:**

$$F_R = \sqrt{310^2 + 260^2 - 2(310)(260) \cos 112.38^\circ} = 474 \text{ lb}$$

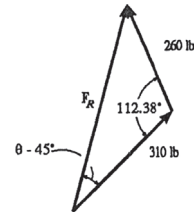
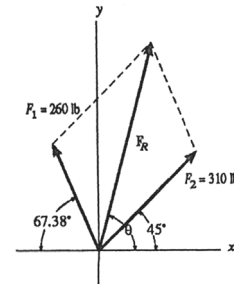
**Sine Law:**

$$\frac{\sin 112.38^\circ}{474} = \frac{\sin(\theta - 45^\circ)}{260} \quad \theta = 75.4^\circ$$



**Ans.**

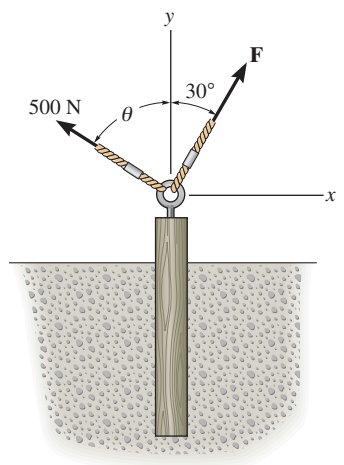
**Ans.**



**Ans:**  
 $F_R = 474 \text{ lb}$   
 $\theta = 75.4^\circ$

**2-3.**

Two forces are applied at the end of a screw eye in order to remove the post. Determine the angle  $\theta$  ( $0^\circ \leq \theta \leq 90^\circ$ ) and the magnitude of force  $\mathbf{F}$  so that the resultant force acting on the post is directed vertically upward and has a magnitude of 750 N.



**SOLUTION**

**Parallelogram Law:** The parallelogram law of addition is shown in Fig. (a).

**Trigonometry:** Using law of sines [Fig. (b)], we have

$$\frac{\sin \phi}{750} = \frac{\sin 30^\circ}{500}$$

$$\sin \phi = 0.750$$

$$\phi = 131.41^\circ \text{ (By observation, } \phi > 90^\circ \text{)}$$

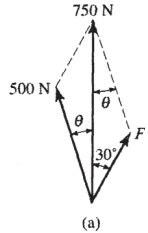
Thus,

$$\theta = 180^\circ - 30^\circ - 131.41^\circ = 18.59^\circ = 18.6^\circ$$

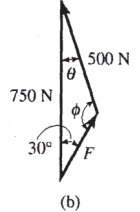
$$\frac{F}{\sin 18.59^\circ} = \frac{500}{\sin 30^\circ}$$

$$F = 319 \text{ N}$$

**Ans.**



**Ans.**



**Ans:**  
 $\theta = 18.6^\circ$   
 $F = 319 \text{ N}$



\*2-4.

Determine the magnitudes of the two components of  $\mathbf{F}$  along members  $AB$  and  $AC$ . Set  $F = 500 \text{ N}$ .

### SOLUTION

**Parallelogram Law:** The parallelogram law of addition is shown in Fig. *a*.

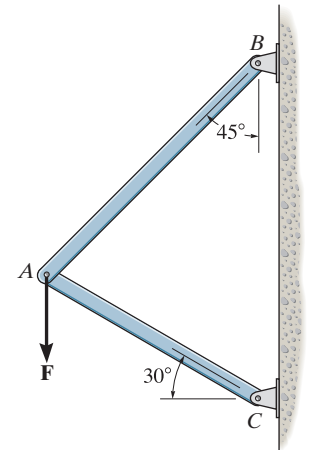
**Trigonometry:** Using the law of sines (Fig. *b*), we have

$$\frac{F_{AB}}{\sin 60^\circ} = \frac{500}{\sin 75^\circ}$$

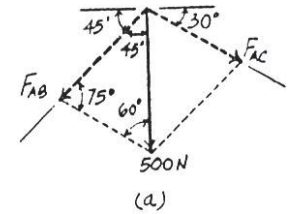
$$F_{AB} = 448 \text{ N}$$

$$\frac{F_{AC}}{\sin 45^\circ} = \frac{500}{\sin 75^\circ}$$

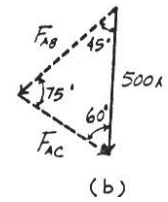
$$F_{AC} = 366 \text{ N}$$



Ans.



Ans.



Ans:

$$F_{AB} = 448 \text{ N}$$

$$F_{AC} = 366 \text{ N}$$

2-5.

Solve Prob. 2-4 with  $F = 350$  lb.

**SOLUTION**

**Parallelogram Law:** The parallelogram law of addition is shown in Fig. *a*.

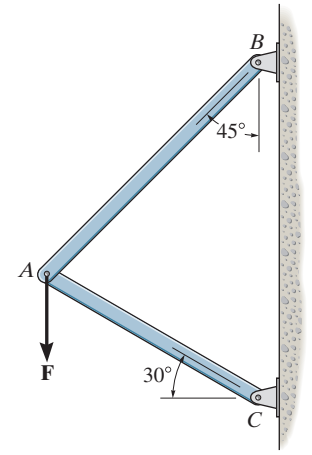
**Trigonometry:** Using the law of sines (Fig. *b*), we have

$$\frac{F_{AB}}{\sin 60^\circ} = \frac{350}{\sin 75^\circ}$$

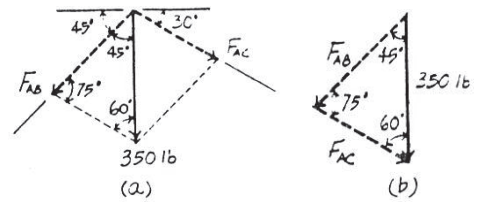
$$F_{AB} = 314 \text{ lb}$$

$$\frac{F_{AC}}{\sin 45^\circ} = \frac{350}{\sin 75^\circ}$$

$$F_{AC} = 256 \text{ lb}$$



**Ans.**



**Ans.**

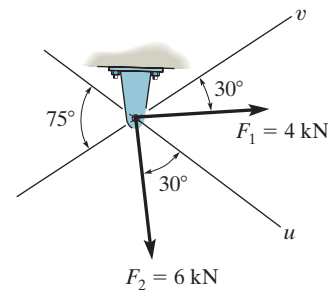
**Ans:**

$$F_{AB} = 314 \text{ lb}$$

$$F_{AC} = 256 \text{ lb}$$

2-6.

Determine the magnitude of the resultant force  $\mathbf{F}_R = \mathbf{F}_1 + \mathbf{F}_2$  and its direction, measured clockwise from the positive  $u$  axis.



**SOLUTION**

**Parallelogram Law:** The parallelogram law of addition is shown in Fig. *a*,

**Trigonometry:** Applying Law of cosines by referring to Fig. *b*,

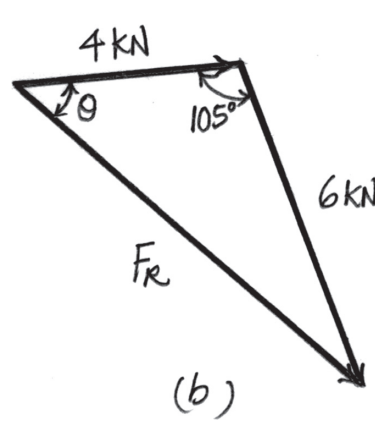
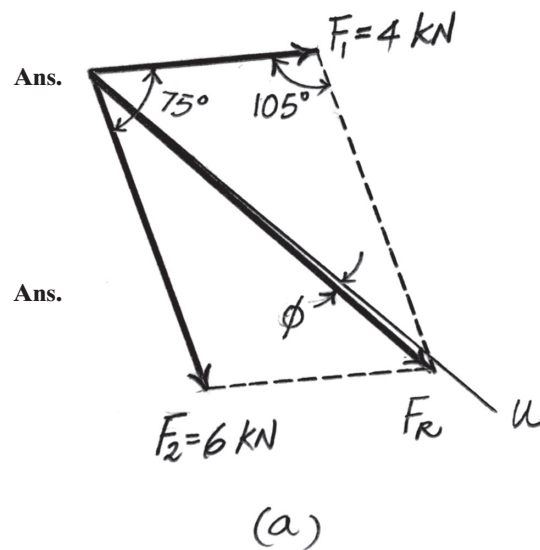
$$F_R = \sqrt{4^2 + 6^2 - 2(4)(6) \cos 105^\circ} = 8.026 \text{ kN} = 8.03 \text{ kN}$$

Using this result to apply Law of sines, Fig. *b*,

$$\frac{\sin \theta}{6} = \frac{\sin 105^\circ}{8.026}; \quad \theta = 46.22^\circ$$

Thus, the direction  $\phi$  of  $\mathbf{F}_R$  measured clockwise from the positive  $u$  axis

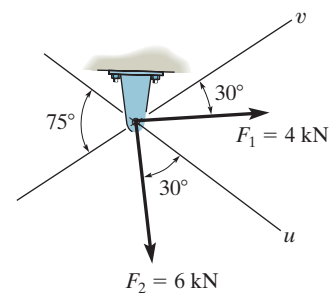
$$\phi = 46.22^\circ - 45^\circ = 1.22^\circ$$



**Ans:**  
 $F_R = 8.03 \text{ kN}$   
 $\phi = 1.22^\circ$

2-7.

Resolve the force  $F_1$  into components acting along the  $u$  and  $v$  axes and determine the magnitudes of the components.



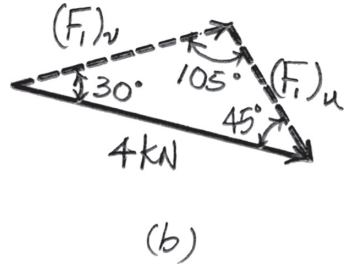
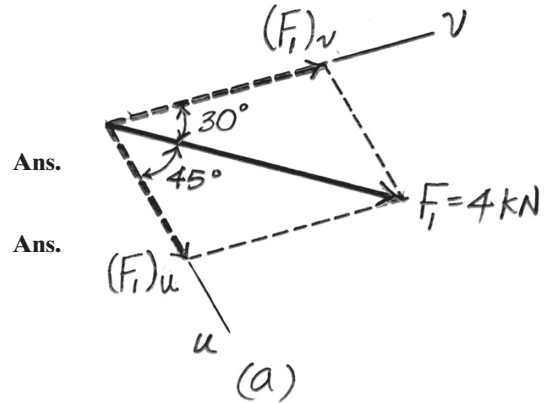
**SOLUTION**

**Parallelogram Law:** The parallelogram law of addition is shown in Fig. *a*.

**Trigonometry:** Applying the sines law by referring to Fig. *b*.

$$\frac{(F_1)_v}{\sin 45^\circ} = \frac{4}{\sin 105^\circ}; \quad (F_1)_v = 2.928 \text{ kN} = 2.93 \text{ kN}$$

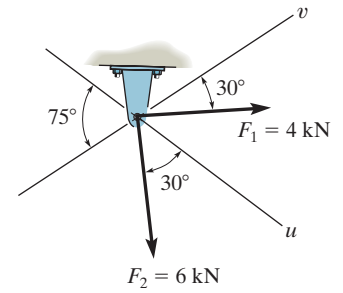
$$\frac{(F_1)_u}{\sin 30^\circ} = \frac{4}{\sin 105^\circ}; \quad (F_1)_u = 2.071 \text{ kN} = 2.07 \text{ kN}$$



**Ans:**  
 $(F_1)_v = 2.93 \text{ kN}$   
 $(F_1)_u = 2.07 \text{ kN}$

\*2-8.

Resolve the force  $F_2$  into components along the  $u$  and  $v$  axes and determine the magnitudes of the components.



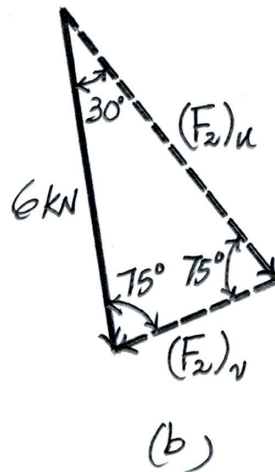
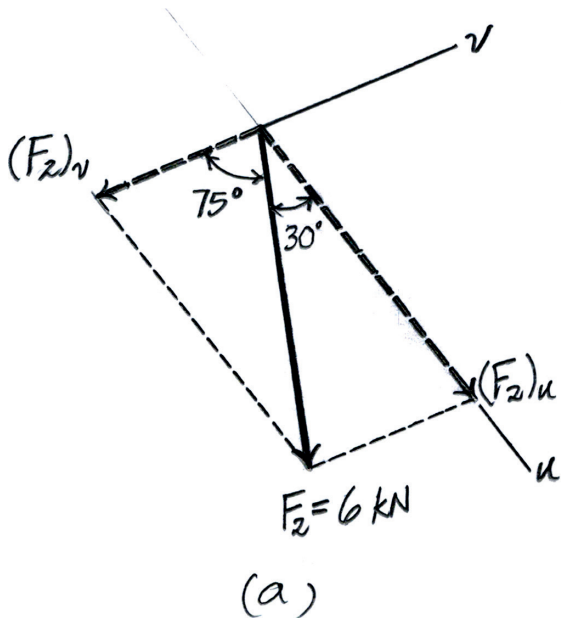
### SOLUTION

**Parallelogram Law:** The parallelogram law of addition is shown in Fig. *a*,

**Trigonometry:** Applying the sines law of referring to Fig. *b*,

$$\frac{(F_2)_u}{\sin 75^\circ} = \frac{6}{\sin 75^\circ}; \quad (F_2)_u = 6.00 \text{ kN} \quad \text{Ans.}$$

$$\frac{(F_2)_v}{\sin 30^\circ} = \frac{6}{\sin 75^\circ}; \quad (F_2)_v = 3.106 \text{ kN} = 3.11 \text{ kN} \quad \text{Ans.}$$



**Ans:**  
 $(F_2)_u = 6.00 \text{ kN}$   
 $(F_2)_v = 3.11 \text{ kN}$

2-9.

Determine the magnitude of the resultant force  $\mathbf{F}_R = \mathbf{F}_1 + \mathbf{F}_2$  and its orientation  $\theta$ , measured clockwise from the positive  $x$  axis.

**SOLUTION**

**Cosine Law:**

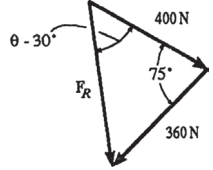
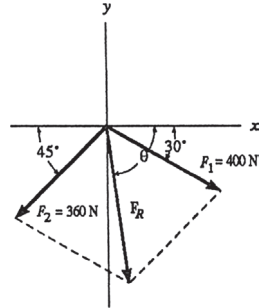
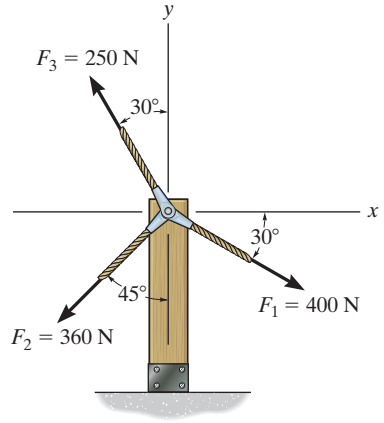
$$F_R = \sqrt{360^2 + 400^2 - 2(360)(400) \cos 75^\circ} = 463.75 = 464 \text{ N}$$

**Ans.**

**Sine Law:**

$$\frac{\sin 75^\circ}{463.75} = \frac{\sin (\theta - 30^\circ)}{360} \quad \theta = 78.6^\circ$$

**Ans.**



**Ans:**  
 $F_R = 464 \text{ N}$   
 $\theta = 78.6^\circ$

**2-10.**

Determine the magnitude of the resultant force  $\mathbf{F}_R = \mathbf{F}_1 + \mathbf{F}_3$  and its orientation  $\theta$ , measured counterclockwise from the positive  $x$  axis.

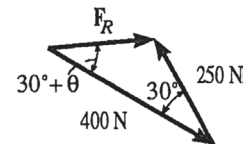
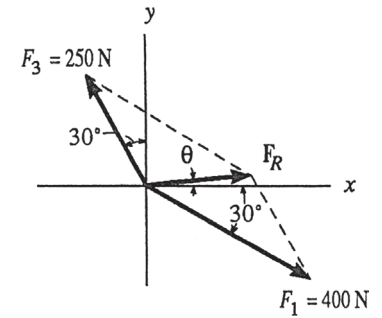
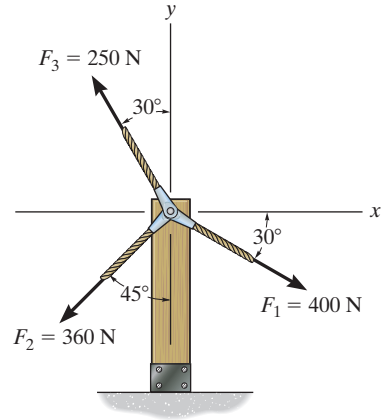
**SOLUTION**

**Cosine Law:**

$$F_R = \sqrt{250^2 + 400^2 - 2(250)(400) \cos 30^\circ} = 222.02 = 222 \text{ N} \quad \text{Ans.}$$

**Sine Law:**

$$\frac{\sin 30^\circ}{222.02} = \frac{\sin (30^\circ + \theta)}{250} \quad \theta = 4.26^\circ \quad \text{Ans.}$$



**Ans:**  
 $F_R = 222 \text{ N}$   
 $\theta = 4.26^\circ$

**2-11.**

If  $\theta = 60^\circ$ , determine the magnitude of the resultant force and its direction measured clockwise from the horizontal.

**SOLUTION**

**Parallelogram Law:** The parallelogram law of addition is shown in Fig. *a*.

**Trigonometry:** Using law of cosines (Fig. *b*), we have

$$F_R = \sqrt{8^2 + 6^2 - 2(8)(6) \cos 100^\circ}$$

$$= 10.80 \text{ kN} = 10.8 \text{ kN}$$

The angle  $\theta$  can be determined using law of sines (Fig. *b*).

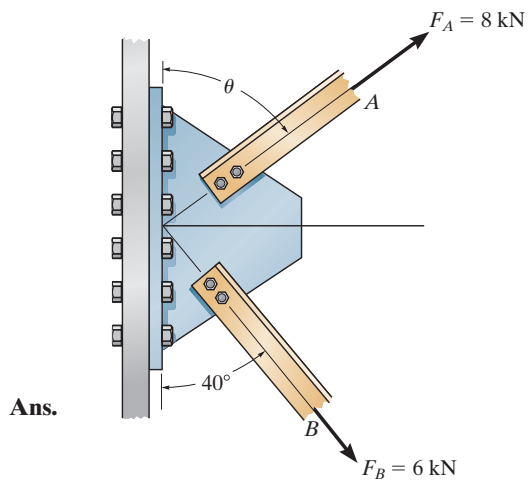
$$\frac{\sin \theta}{6} = \frac{\sin 100^\circ}{10.80}$$

$$\sin \theta = 0.5470$$

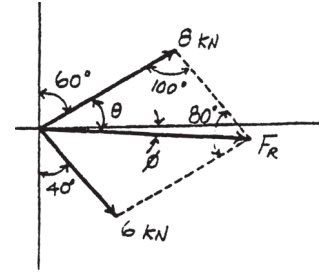
$$\theta = 33.16^\circ$$

Thus, the direction  $\phi$  of  $F_R$  measured from the  $x$  axis is

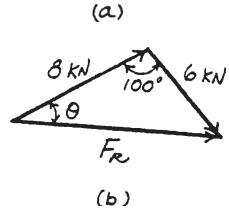
$$\phi = 33.16^\circ - 30^\circ = 3.16^\circ$$



**Ans.**



**Ans.**



**Ans:**  
 $F_R = 10.8 \text{ kN}$   
 $\phi = 3.16^\circ$